Enhanced consolidation in brittle geomaterials susceptible to damage

A. T. Mahyari and A. P. S. Selvadurai*

Department of Ci il Engineering and Applied Mechanics, McGill Uni ersity, 817 Sherbrooke Street West, Montreal, Q.C., Canada H3A 2K6

SUMMARY

This paper examines consolidation behaviour of saturated geomaterials with a matrix component which is susceptible to damage. Finite-element-based computational model accounts for the alteration in both the deformability and permeability characteristics of the porous material due to damage evolution. The isotropic damage criteria governing the evolution of elastic stixness and hydraulic conductivity parameters are characterized by the dependency of the damage variable on the distortional strain invariant. The computational procedure is utilized to evaluate the extent to which the time-dependent axisymmetric indentation behaviour of a rigid circular punch on a poroelastic half-space can be inßuenced by the damage evolution in the porous skeleton. (1998 John Wiley & Sons, Ltd.

KEY WORDS: poroelasticity; isotropic damage; brittle geomaterials; enhanced consolidation; saturated geomaterials; computational modelling; indentation of geomaterials

1. INTRODUCTION

The classical theory of poroelasticity developed by Biot^{1, 2} examines the coupled behaviour of ßuid ßow and elastic deformations on the consolidation process of porous materials saturated with either incompressible or compressible pore ßuids. The theory of poroelasticity has been successfully applied to examine time-dependent transient phenomena in a variety of natural and synthetic materials, including geomaterials and biomaterials.³ The assumption of linear elastic behaviour of the porous skeleton is a signiPcant limitation in the application of the classical theory of poroelasticity to brittle geomaterials which could exhibit sti¤ness changes and, in particular, elastic sti¤ness degradation in the constitutive behaviour of the skeleton of the geomaterial. This non-linear behaviour can be due to development of microcracks and microvoids in the porous fabric of the geomaterial which essentially retains its elastic nature (i.e. absence of irreversible plasticity phenomena). Such damage or microvoid and microcrack evolution can result in the alteration of the permeability characteristics of the porous medium. The e¤ect of such and on either the degradation of elastic moduli, and in extreme situations,

0(mthelrs201d) J538 (2gso) 2223 (0i2) S8 c(pa (eit 192) d538 (203) TD 2 logilliads b) OTO / 654k la 166 JTT / 4594 (063) 1643 / 759 / 754 TID (3017) 6

on concrete. The theory of damage mechanics has been extensively applied to model the behaviour of such brittle geomaterials. The exect of microcrack developments on permeability characteristics of saturated geomaterials has also been observed by Zoback and Byerlee, Shiping and Kiyama and Siyama and Hover in concrete.

When considering saturated poroelastic geomaterials, their consolidation response can be inßuenced by the evolution of damage in the porous skeleton. The notion of continuum damage is considered to be more relevant to geomaterials such as soft rocks and overconsolidated clays sense can occur due to generation of microvoids or were progressive softening in an microcracks. The classical theory of continuum damage mechanics¹⁵ can be extended to model such damage phenomena in porous saturated materials. This theory simulates the exect of microcrack developments on the behaviour of materials prior to the development of (i.e. fractures). In such modelling, damage is interpreted as a reduction in the sti¤ness of the material due to the generation of microcracks and other microdefects. In this study attention is of material where the associated damage processes restricted primarily to . / . . before inception of strain softening (i.e. strictly pre-peak elastic behaviour) can be described by an isotropic damage model. Admittedly, the damage processes are expected to be highly anisotropic in nature and could invariably be restricted to localized zones. The exect of soil skeletal damage on the consolidation behaviour of saturated geomaterials can be examined by representing the sti¤ness properties and the permeability characteristics of porous medium as a function of the state of damage in the saturated geomaterial. Cheng and Dusseault¹⁶ developed an anisotropic damage model to examine the poroelastic behaviour of saturated geomaterials. Their studies were, however restricted to the case where there was no corresponding evolution in the permeability characteristics of the geomaterials during the damage processes.

In this study a Pnite element technique is used to examine the inßuence of damage-induced alterations in both the elastic sti¤ness and the permeability characteristics of the porous geomaterial on the corresponding consolidation response of a saturated poroelastic medium. The isotropic damage evolution law used in the analysis is characterized by the dependency of damage parameters on the distortional strain invariant. Two di¤erent phenomenological damage criteria(a)-220(saturated geomaterials procedure islutalized to valuaite the exthint crothedependent behaviour of a apermeatle res2e a poroelastion be inßuencdc by the damage evolution

2. GOVERNING EQUATIONS

$$\sigma_{ij}^{"} = \frac{2\mu v}{1! - 2v} \varepsilon_{kk} \delta_{ij}^{\#} = 2\mu \varepsilon_{ij}! - \frac{3(v_{u}! - v)}{(1! - 2v)(1 \# - v_{u})}, \delta_{ij}$$

$$= \frac{2\mu^{-2} (1! - 2v)(1 \# - v_{u})^{2}}{9(v_{u}! - v)(1! - 2v_{u})} \zeta_{v}! - 2\mu^{-} (1 \# - v_{u})$$
(1a)

3. FINITE ELEMENT FORMULATIONS

Finite element methods have been widely applied for the study of problems in poroelasticity (see e.g. References 18, 20). Reviews of both analytical and numerical approaches to the study of soil consolidation related to poroelastic media are given by Lewis and Schreßer

developments, the theory	y of continuum da	mage mechanics h	as been widely us	ed to predict the

that damage evolution is a function of the shear strain energy and proposed the following damage evolution equation for rocks:

$$\frac{\partial_{\prime}}{\partial \xi_{d}} = \eta \frac{\gamma \xi_{d}}{1 \# \gamma \xi_{d}} \left(1! - \frac{\gamma}{\zeta_{d}} \right)$$
 (9)

where the equivalent shear strain ξ_d is dePned as

$$\xi_{\rm d}$$
" $(i_{ij})^{1/2}$, i_{ij} " ε_{ij} ! $\frac{1}{3}\varepsilon_{kk}\delta_{ij}$ (10)

and η, γ are material constants which are positive. In this formulation, the normalizing damage measure is the critical damage χ_c which is associated with the damage corresponding to a residual value of the strength of the geomaterial under uniaxial compression. We note that χ_c need not be the only normalizing variable; the formulation can be presented in terms of χ_p the damage at peak loads which can limit the development of localization expects that can result when χ_c P χ_c .

For saturated geomaterials susceptible to damage, the elastic properties and permeability characteristics can alter due to development of microcracks in the porous fabric.

4.1. Deformability characteristics

The constitutive parameters applicable to an isotropic poroelastic material which experiences micromechanical damage in the porous fabric can be represented as a function of intact elastic properties by invoking the hypothesis of strain equivalence.³¹ The generalized constitutive tensor applicable to damaged materials which exhibit isotropic damage takes the form

$$\int_{ijkl}^{d} (1! \ /)_{ijkl} (" 1,...,4, " 1,...,4)$$
 (11)

where $_{ijkl}$ is the elasticity tensor applicable to virgin elastic materials (see e.g. Reference 33). The damage evolution law can specify the variation of the damage variable ($_{\cdot}$) with the state of strain in material. The damage evolution law proposed by Cheng and Dusseault¹⁶ is employed in this study to model the elastic stipness degradation of materials. The evolution of damage variable can be obtained by the integration of (9) (between the limits $_{\cdot}$ 0 to $_{\cdot}$) as follows:

" , c! (, c! , 0)(1#
$$\gamma \xi_{\rm d}$$
) ^{$\eta/\gamma D_{\rm c}$} exp(! $\eta \xi_{\rm d}$ /, c) (12)

where $_{0}$ is the initial value of damage variable corresponding to intact state of material (e.g. $_{0}$ " 0 for virgin state of materials).

4.2. Hydraulic conducti ity characteristics

Development of damage criteria which can account for alterations in the hydraulic conductivity during evolution of damage in saturated geomaterials is necessary for computational modelling of such phenomena in poroelastic media. Literature on the coupling between microcrack developments and permeability evolution in saturated geomaterials is primarily restricted to experimental observations. The exect of microcrack development on the permeability characteristics of Buid saturated geomaterial was Prst investigated by Zoback and



Figure 3. Permeability evolution in saturated geomaterials (a) after Zoback and Byerlee; 11 and (b) after Shiping 12.

Byerlee, 11 who conducted triaxial tests on granite. Figure 3 illustrates their experimental observations which indicate that the permeability coe | cient is Prst reduced slightly due to

5. COMPUTATIONAL PROCEDURES AND NUMERICAL RESULTS
The exect of soil skeletal damage on the time-dependent poroelastic behaviour of saturated

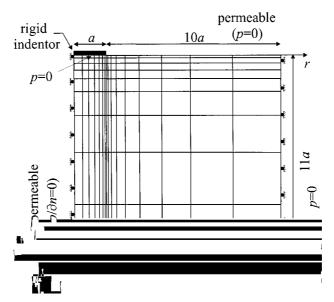


Figure 5. Finite element discretizations

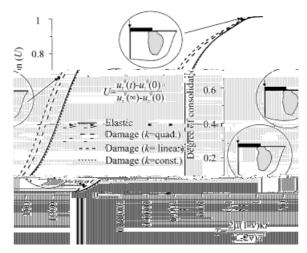


Figure 6. Degree of consolidation and evolution of damaged zone (where , /, c' 0.05) with time

conductivity is maximum. Figure 6 also indicates that much of the damage generation takes place instantaneously and further pore pressure di¤usion which results in the change of e¤ective stresses, does not appreciably alter the extent of damage. Admittedly no generalizations can be made of this observation since the rate of load transfer will depend on the prescribed damage evolution laws.

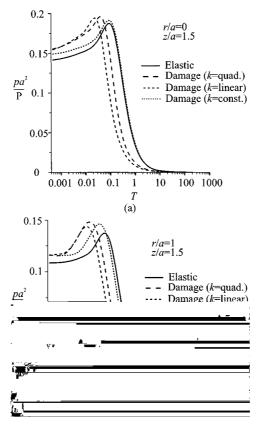


Figure 7. Pore pressure evolution at di¤erent depths

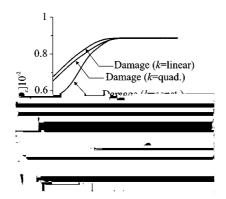


Figure 8. Evolution of damage variable at the edge of indentor

Figure 7 illustrates the evolution of pore pressure at two locations of the indentor; the centre of indentor (/ " 0) and the edge of indentor (/ " 1) corresponding to a depth of / " 1·5 within the poroelastic half-space. The damage models predict higher excess pore pressures in the porous medium which is consistent with observations by Cheng and Dusseault. 16 The evolution of the

damage variable with time at the edge of indentor ($^{\prime}$ / $^{"}$ 1) at a depth of $^{\prime}$ / $^{"}$ 0·1 is also shown in Figure 8.

6. CONCLUDING REMARKS

The classical theory of poroelasticity for a Buid saturated brittle geomaterial has been extended through computational modelling to include the inßuence of both damage evolution in the geomaterial fabric and alterations in the Buid transport behaviour due to damage evolution. This latter modiPcation to the modelling is considered to be a novel development in the application of damage mechanics concepts to the study of poroelastic phenomena. The studies to date are based on plausible damage evolution laws which are derived from a limited database of experimental results. The damage evolution laws based on micromechanical considerations, on the other hand, will require considerably more analytical exorts and the incorporation of the possible inßuences of scale at which micromechanical processes generate microcrack evolution which manifests in the form of damage. The procedure applied in this paper is intended to capture phenomenological processes which can be modelled by appeal to experimentation. The computational modelling of damage evolution in the geomaterial fabric and the alteration in the hydraulic transport characteristics can be easily accomodated with a conventional formulation of computational modelling of transient processes in poroelastic media. The indentation problem modelled in this paper illustrates an example where damage evolution and permeability alterations can occur in zones of high local contact stresses. The modelling strictly excludes the possible development of strain localization phenomena. It is appreciated that such strain localization phenomena can contribute to both non-homogeneity and anisotropy in the permeability characteristics which merits further consideration. Also, the incorporation of such localization exects will require a consistent formulation of the computational scheme to account for scale exects, numerical stability and mesh dependency (see e.g. Reference 34). The numerical results presented in the paper illustrate the various inßuences of geomaterial skeletal softening and alterations in the hydraulic transport characteristics on the consolidation rate for the indentor. For the damage laws considered in this paper, the inßuence of hydraulic property alterations due to damage

7. J. Mazars, ÔMechanical damage and fracture of concrete structures 0
8. J. C. Simo and J. W. Ju, &train- and stress-based continuum damage models-II. Computational aspects 0
9. S. Yazdani and H. L. Schreyer, ÔAnisotropic damage model with dilation for concrete (1988).
10. R. de Borst, J. Piman, R. H. J. Peerlings and L. J. Sluys, ©n gradient-enhanced damage and plasticity models for failure in quasi-brittle and frictional materials § 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
11. M. D. Zoback and J. D. Byerlee, $\hat{0}$ The exect of microcrack dilatancy on the permeability of Westerly Granite $\hat{0}$ 0, 752 755 (1975).
12. L. Shiping, L. Yushou, L. Yi, W. Zhenye and Z. Gang, Permeability-strain equations corresponding to the complete
stress strain path of Yinzhuang Sandstone (Indiana)
., pp. 1643-1650, 1996. 14. H. R. Samaha and K. C. Hover, Ûnßuence of microcracking on the mass transport properties of concrete0
., , 416. 424 (1992). 15. L. M. Kachanov, ÕTime of rupture process under creep conditionsÕ
16. H. Cheng and M. B. Dusseault, Deformation and di¤usion behaviour in a solid experiencing damage: a continuous damage model and its numerical implementation 0, 0, 1323–1331 (1993).
17. J. R. Rice and M. P. Cleary, & Some basic stress diausion solution for Buid-saturated elastic porous media with compressible constituents 0,
18. R. S. Sandhu and E. L. Wilson, Finite element analysis of Bow in saturated porous media 0
 J. Ghaboussi and E. L. Wilson, Œlow of compressible βuid in porous elastic media Q
20. J. R. Booker and J. C. Small, ÔAn investigation of the stability of numerical solution of Biotos equations of consolidation 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
21. R. W. Lewis and B. A. Schreßer, "
22. A. P. S. Selvadurai and T. S. Nguyen, @Computational modelling of isothermal consolidation of fractured porous media@ / , 1 , 39 , 73 (1995).
23. I.M. Smith and D. V. Gri¦ ths, Wiley, New York, 1988. 24. D. Krajcinovic and G. U. Fonseka, 0The continuous damage theory of brittle materials 0 , 809. 815
(1981). 25. D. Krajcinovic, ĈContinuous damage mechanicsÕ , , 1 6 (1984).
26. A. P. S. Selvadurai, © ransverse loading of unidirectionally reinforced composites: the role of matrix fracture in ASME, New York; D.H. Allen and J.W. Ju eds, Vol. 1 , pp. 117 127, 1994.
27.J0(Gr49(H190-269(Descriplidati1y)-499(221-26365(ropinov18)-256(damag,)-aD(umelidati1.)-to9(222(elasticabitureÑ6-382(in)]TJ/F2